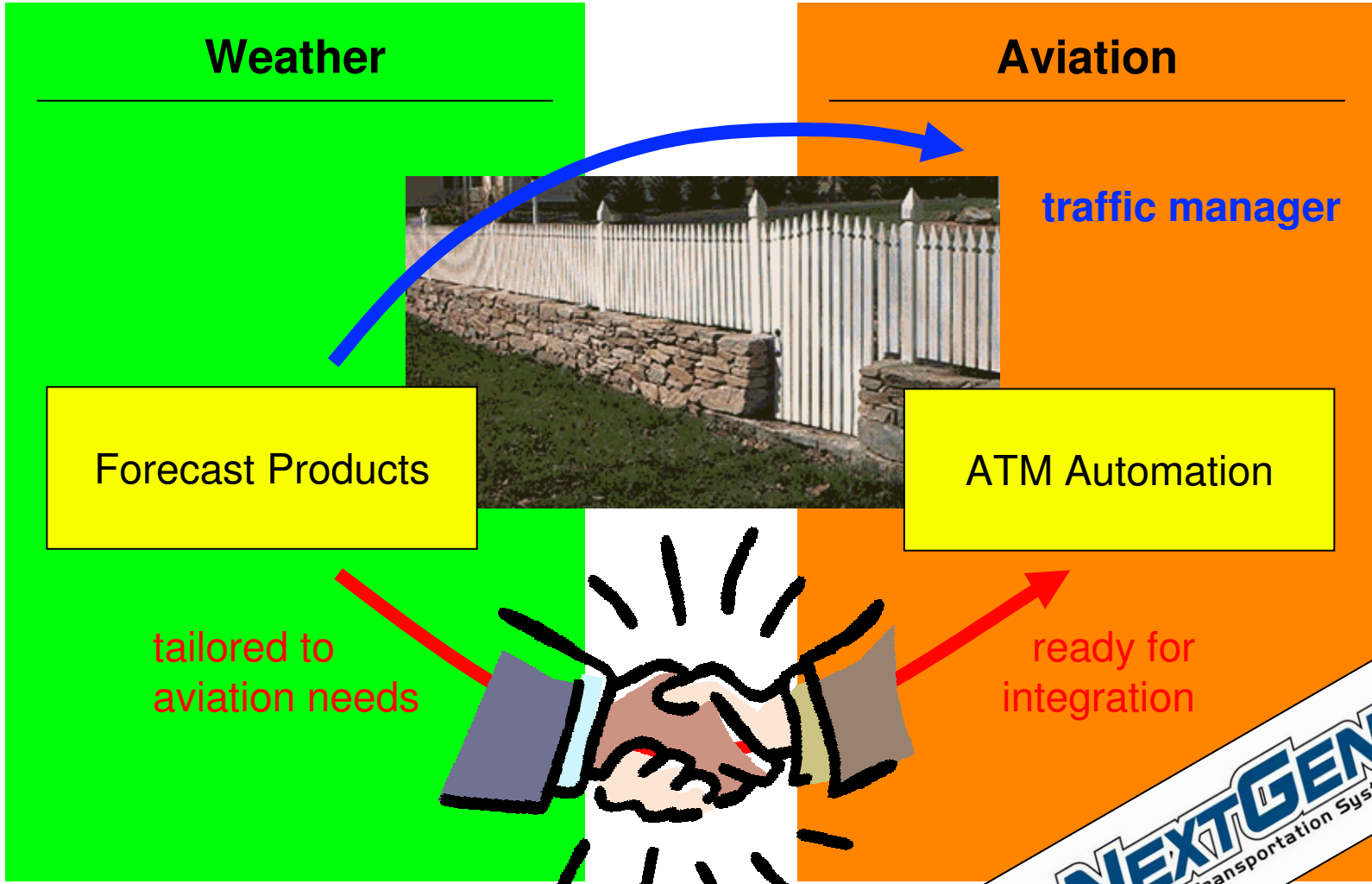


Weather Impact Modeling

Based on
Joe Mitchell's slides

Old Paradigm: Human Centric

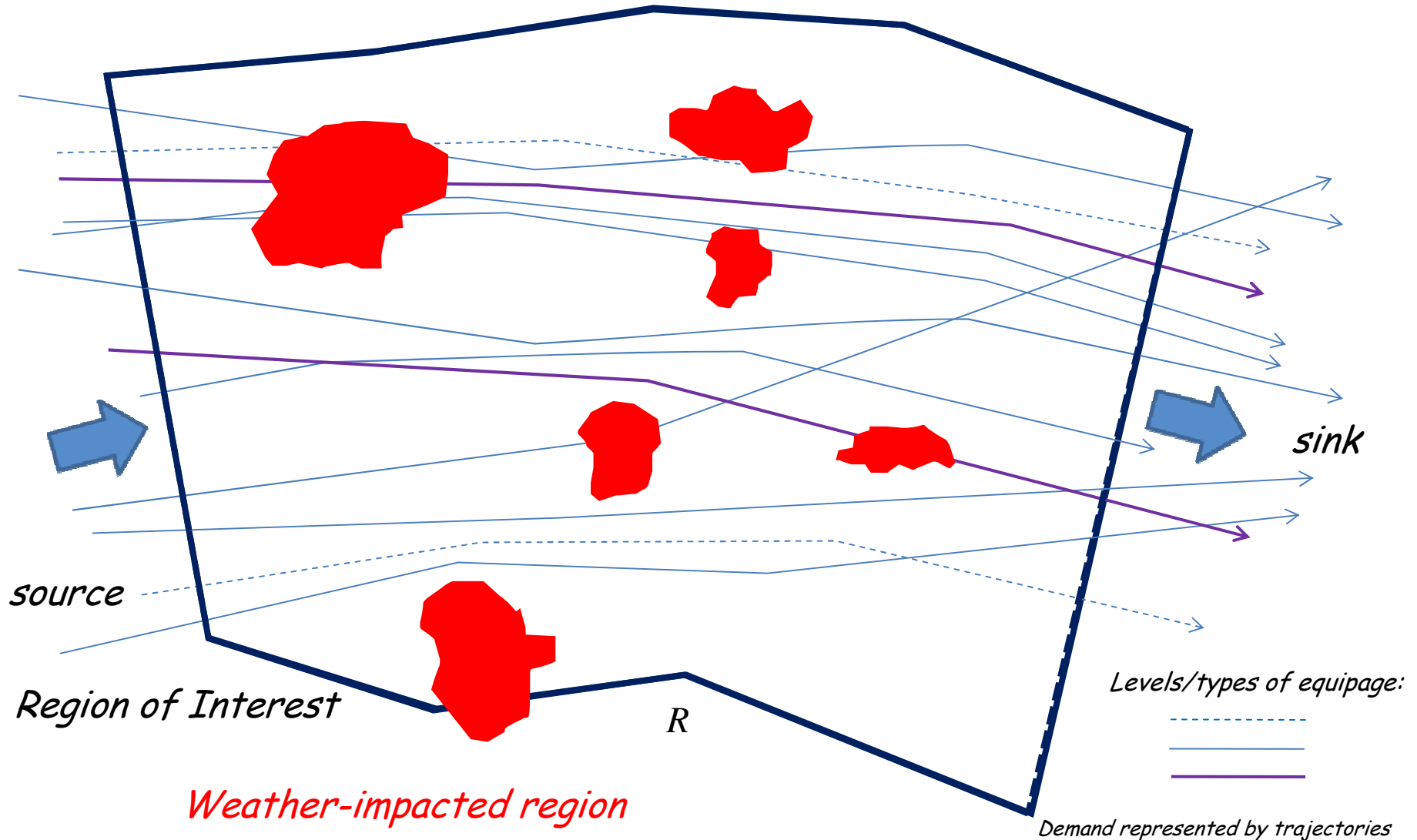


New Paradigm: Automation Centric



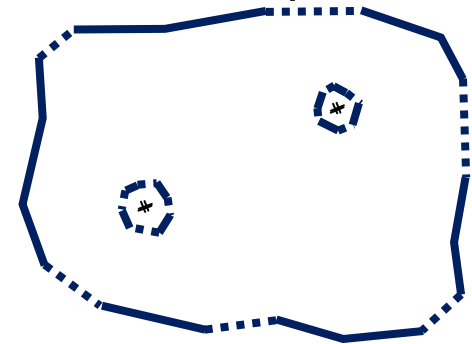
Basic En Route Model

Modeling the impact of weather on capacity of airspace



Inputs: Region of Interest

- Region of airspace, R
- Subset of 2D space (polygonal domain)
- Subset of surface of sphere
- Subset of 3D space



Inputs: Time Horizon

- Time window, $[t_1, t_2]$, of interest
- Sliding time window $[t_1, t_2]$
- Updates every Δt



Inputs: Demand

- “Demand” given as a set of trajectories (flights) in space-time:

$$\tau : (x_1, y_1, z_1, t_1), (x_2, y_2, z_2, t_2), (x_3, y_3, z_3, t_3), \dots$$

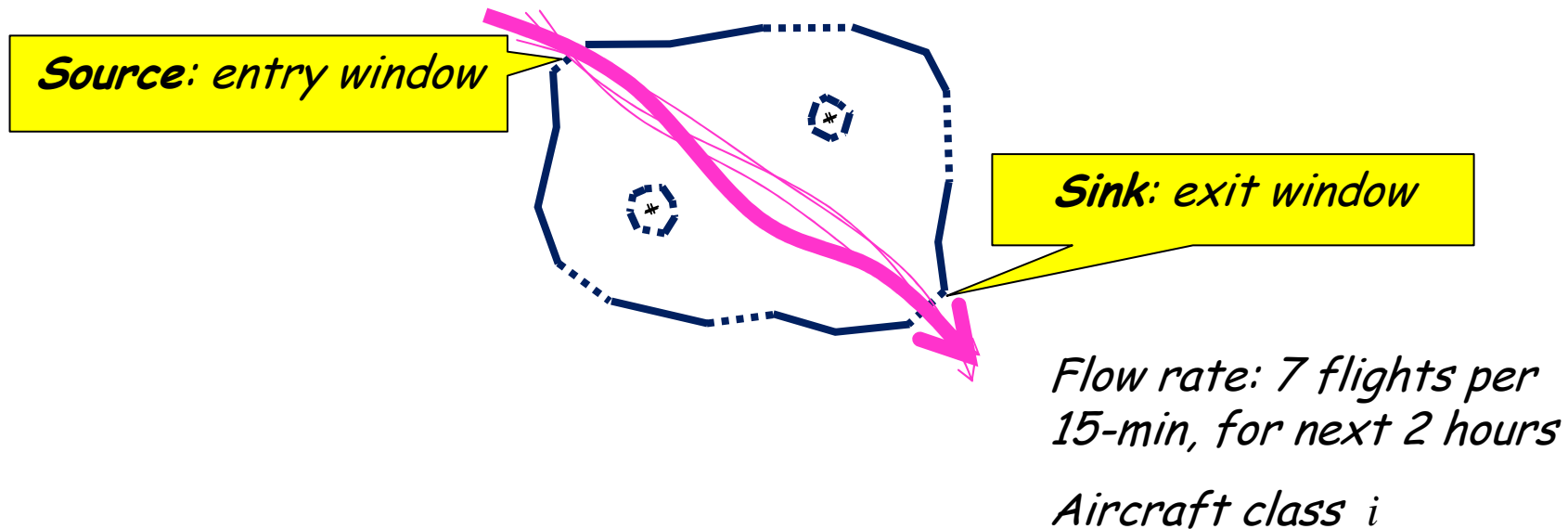
- Each trajectory τ has associated with it
 - Probability distribution of time T_τ when τ enters R
 - Given by ETA estimator
 - Equipage class, i , which includes information about the aircraft, specifying a set Σ_i of preferences and parameters
 - Priority, specified as an integer $\in \{1, 2, \dots, N_p\}$
 - Entrance point (or window), where it enters R
 - Exit point (or window) where it will leave R



*More detail
below*

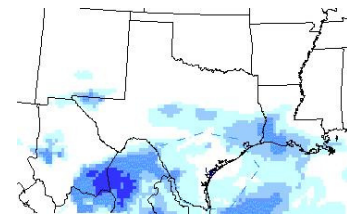
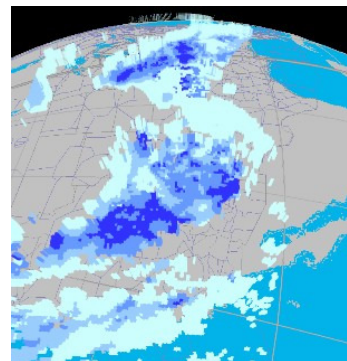
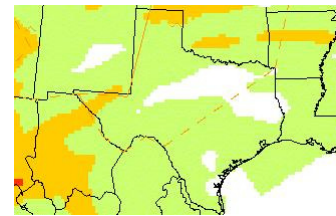
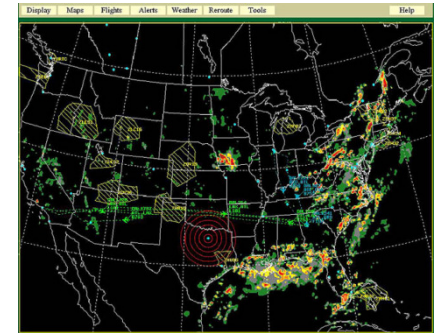
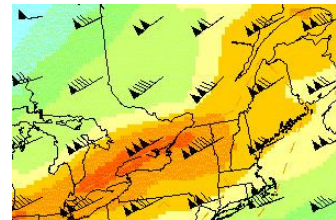
Inputs: Demand

- Demand can be approximated be an aggregation of trajectories into flows, bucketed by time:



Inputs: Weather

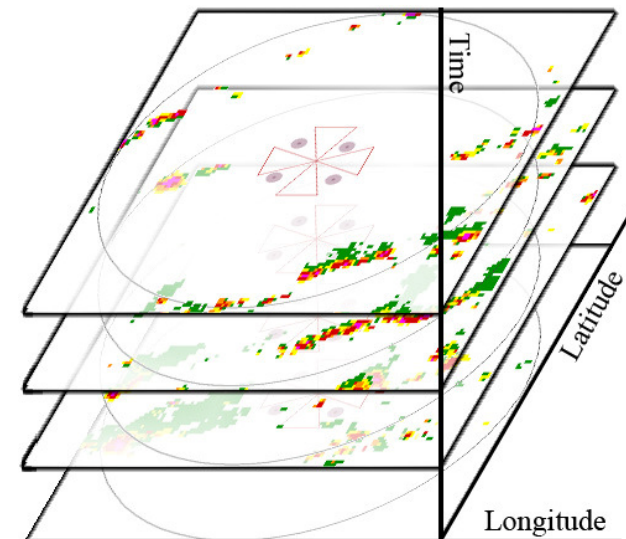
- There are many types of weather events:
 - Convection
 - Icing conditions
 - Turbulence
 - Fog/Impeded visibility
 - Volcanic ash
- Let j indicate the **type** of weather event



Inputs: Weather

- Each type j of weather event:
 - $W_j(x,y,z,t) = \text{intensity}$ at position (x,y,z) , time t
 - $W_j(x,y,z,t)$ is not known with certainty, but is given by a probabilistic forecast
 - Binary impacts: $W_j(x,y,z,t) \in \{0,1\}$
- **Impact region** of weather event j for class i aircraft:
 - $I_{i,j}(t) = \{ (x,y,z) : W_j(x,y,z,t) \geq \xi_{i,j} \}$
- Since impact regions can vary over time (dynamic weather), it is best to view impact regions as portions of space-time.

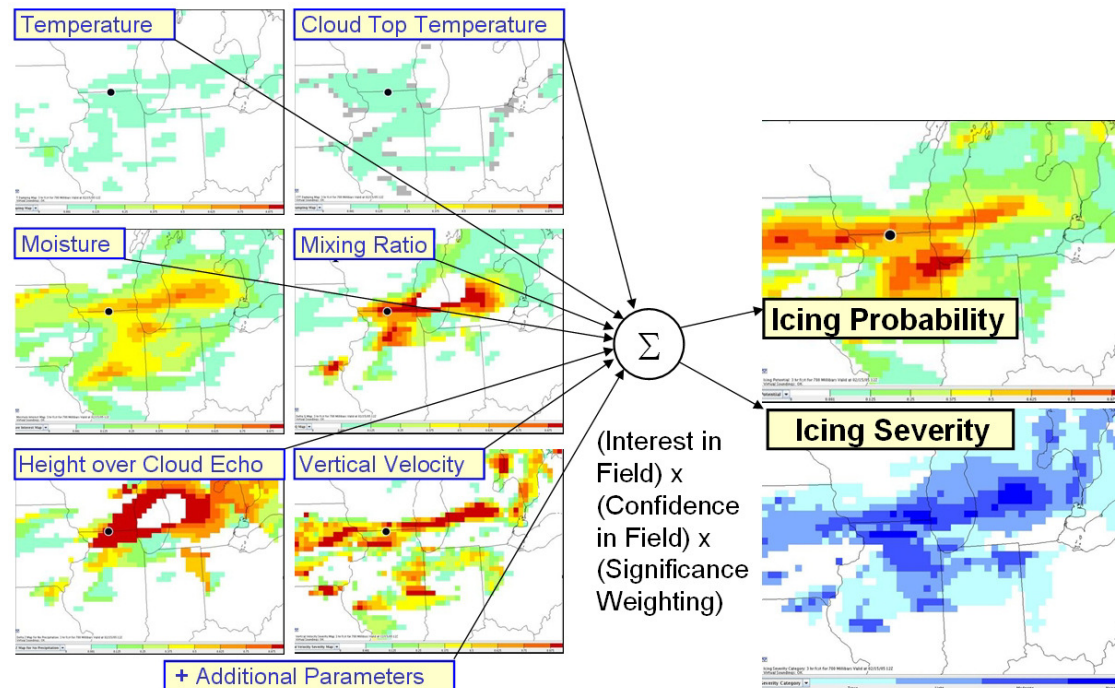
The event either exists or it does not



Convective example

Inputs: Weather

- Each type j of weather event may have many forms of data input that yield the intensity map, $W_j(x, y, z, t)$
- Example: Icing



Weather Impacts on Routes

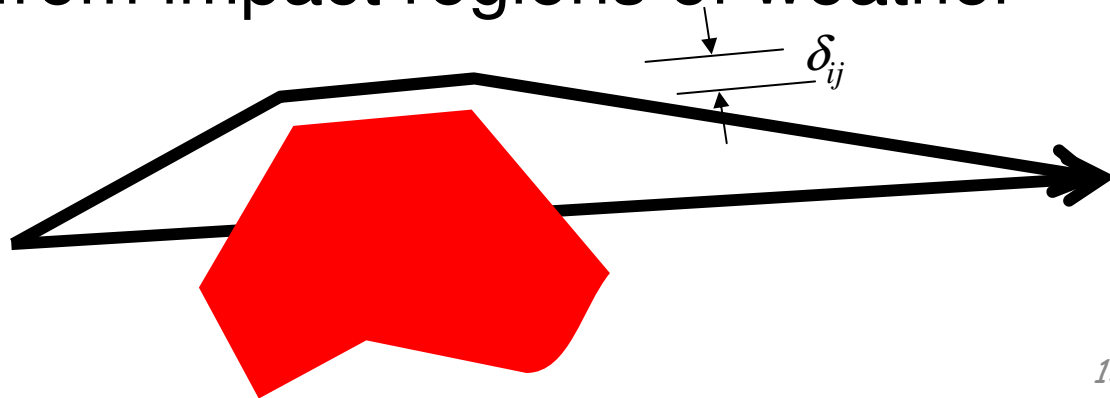
- “No-Go” constraints (avoidance model)
- Cost related to intensity/severity
- Limited total exposure
- Limited exposure bursts

Weather Impacts on Routes: “No-Go” Constraints

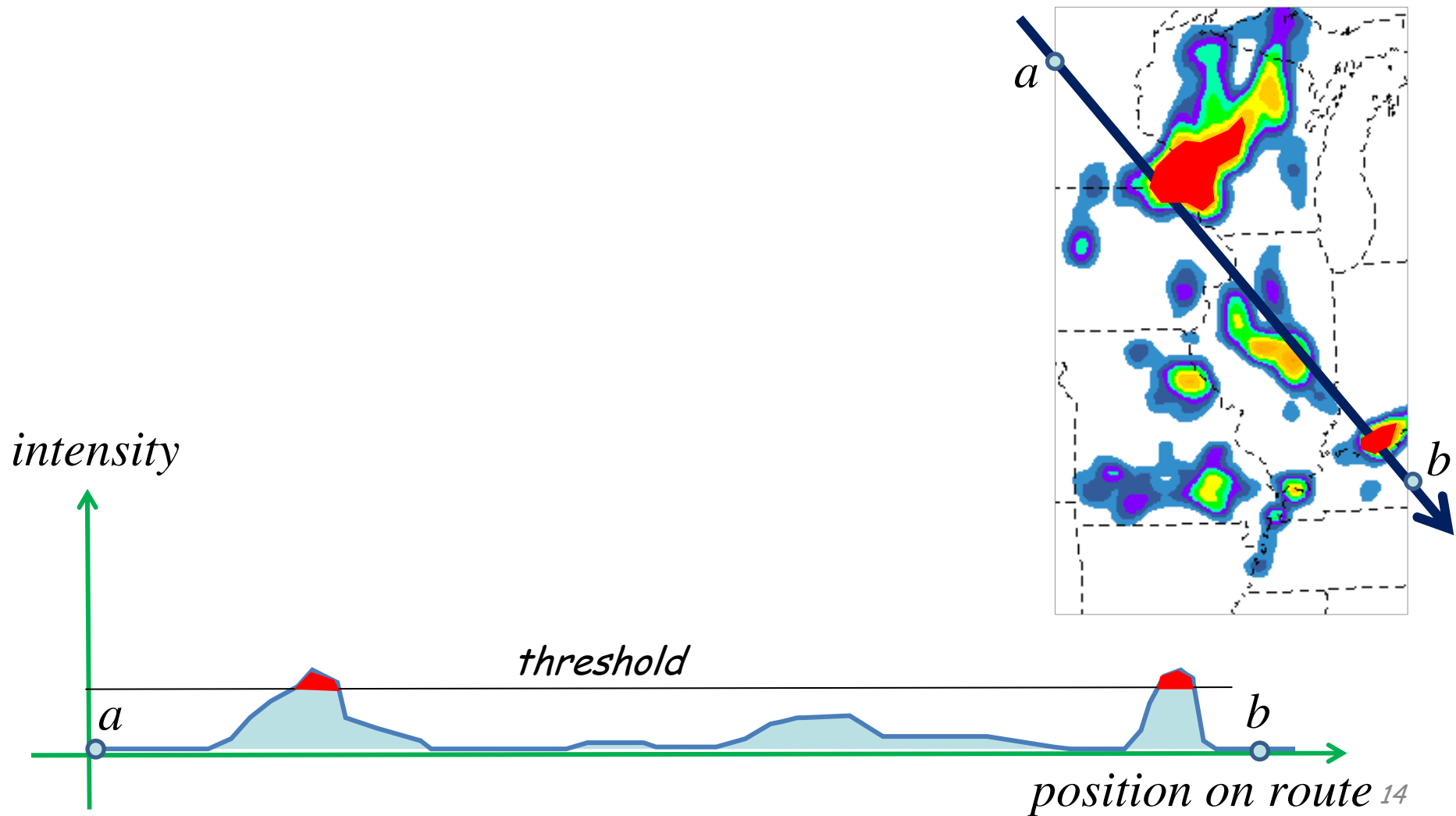
- Impact regions are “no-go” constraints
 - Routes *must* avoid regions whose intensity values are above a specified threshold, $\alpha_{i,j}$.
 - Optionally, there is a weather avoidance threshold, $\delta_{i,j}$, specifying a minimum clearance distance a route of equipage class i should stay from impact regions of weather type j .

Also: Clearance above (in z) echo top

Hard constraint



Example: No-Go Above a Threshold



Weather Impacts on Routes: Function of Intensity/Severity

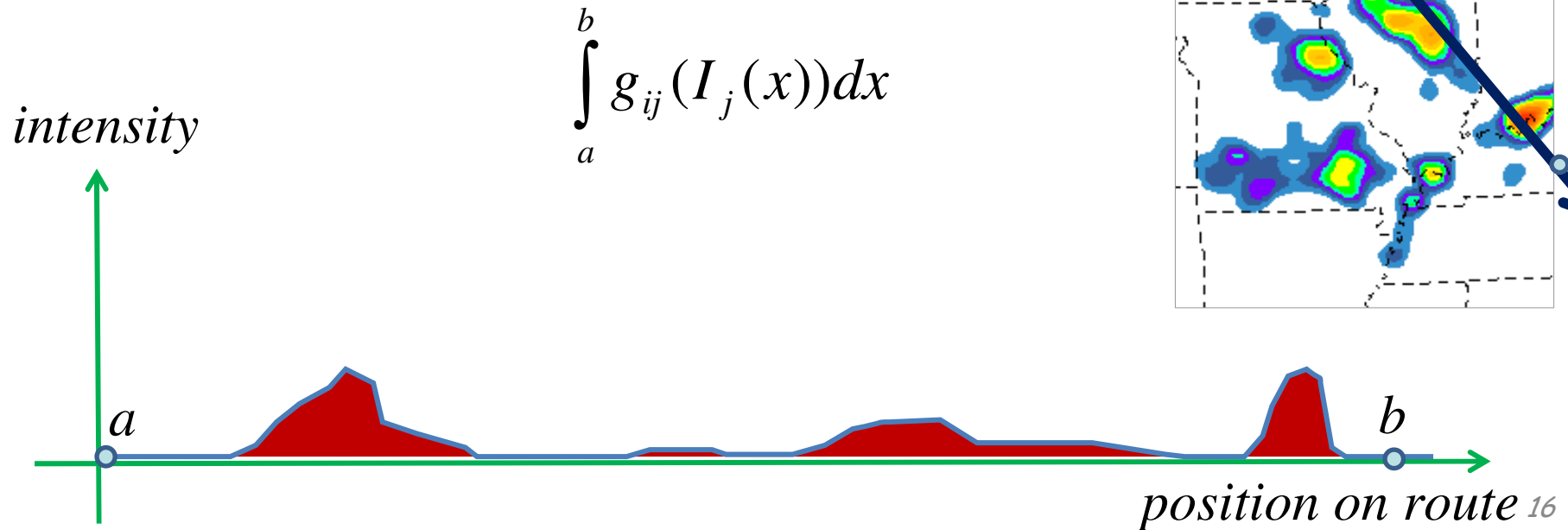
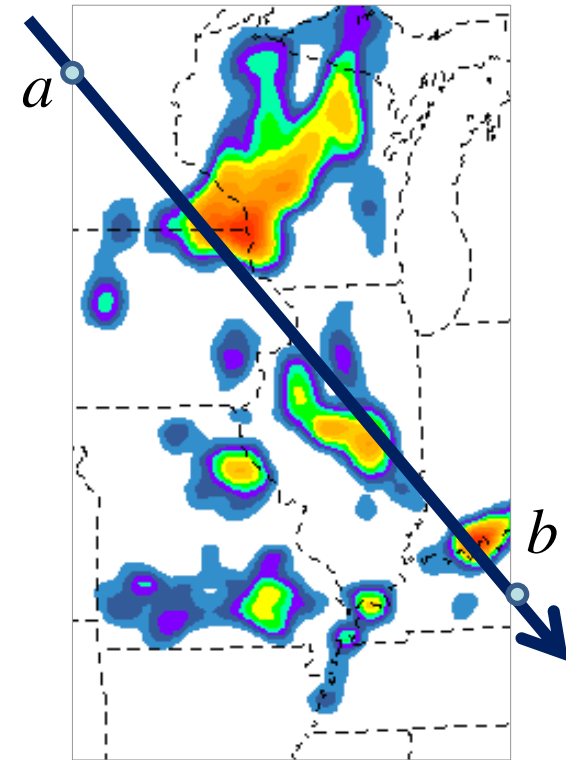
- Impact regions incur cost related to intensity along the route from a to b :
 - Intensity $I_j(x)$ at position x implies cost per unit distance of $g_{ij}(I_j(x))$, for a total cost of

$$\int_a^b g_{ij}(I_j(x))dx$$

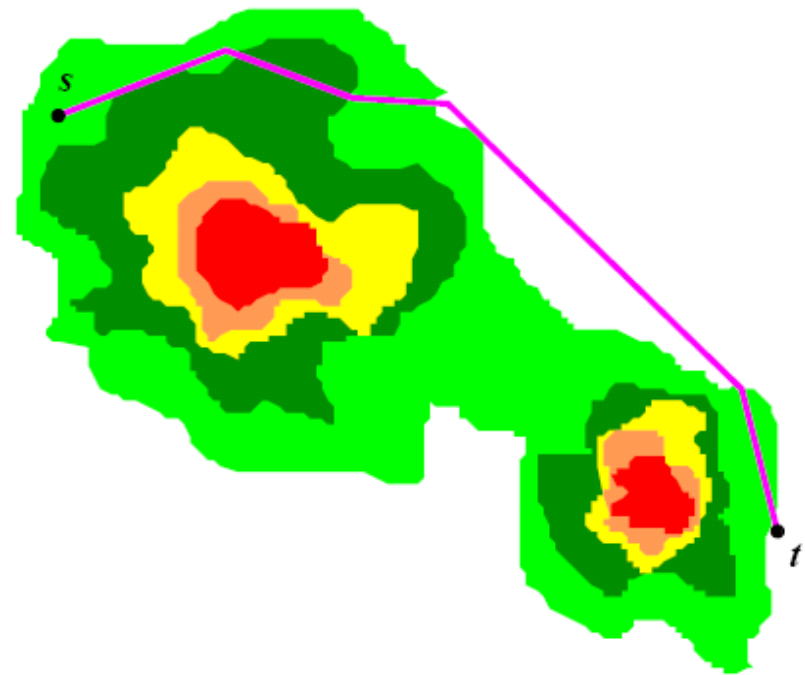
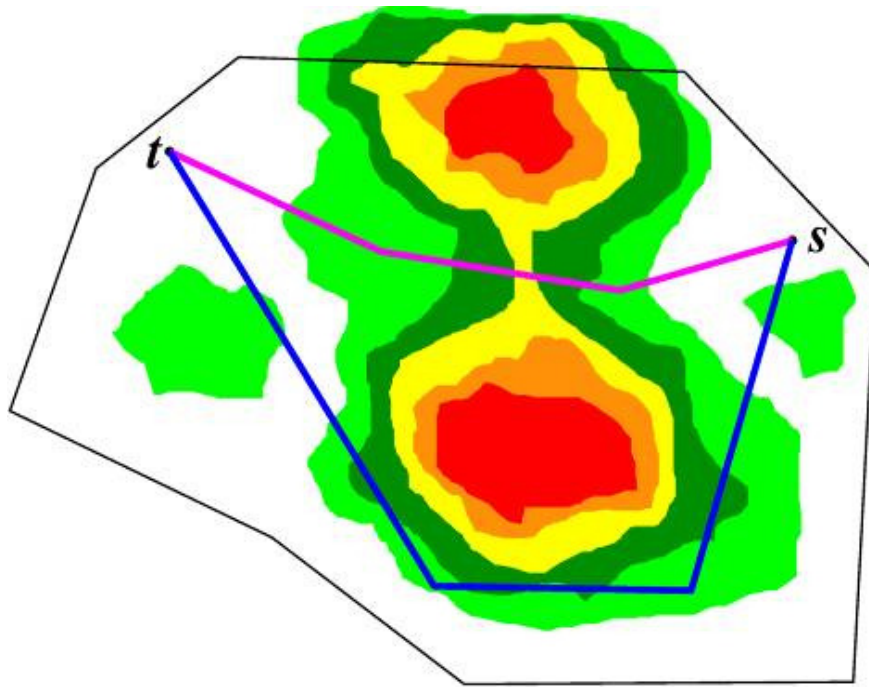
Can also take into account the probabilities associated with the weather event - stochastic model

Example: Weighted Impact Cost

Route is feasible, but incurs a cost related to the integrated intensity along the route



Example: Weighted Impact Costs

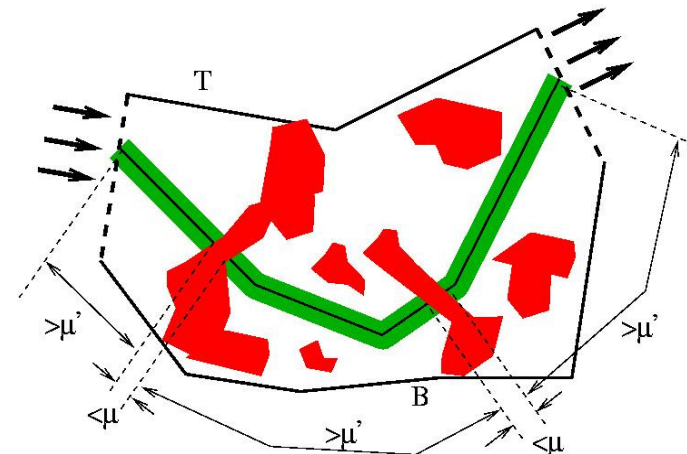
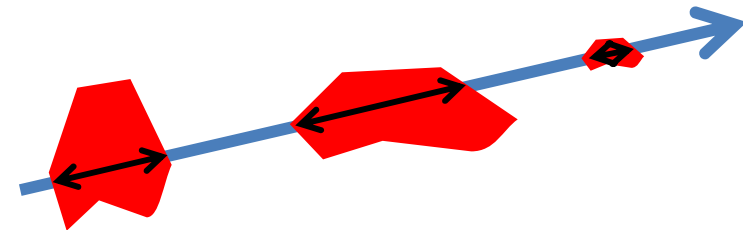


Weather Impacts on Routes: Limited Exposure

- Impact regions incur cost related to intensity along the route from a to b :
 - Total exposure parameter: Total travel (throughout R) cannot exceed $D_{i,j}^{max}$

– Alternation parameters:

- Can travel $\leq d_{i,j}$ in region of type j if followed by travel of $\geq D_{i,j}$ outside regions of type j
- $\mu = d_{i,j}$ $\mu' = D_{i,j}$



Discussion: Do these limited exposure models reflect any actual aircraft-weather interactions?

Inputs: Set Σ_i of Preferences/Parameters

- RNP parameter, $\delta_{RNP,i}$, specifying how closely an aircraft of class i can follow a specified route
- For each type j of weather constraint, and for each equipage class i :
 - Offset (clearance) $\varepsilon_{i,j}$ to be applied to type j impact regions to be treated as “no-go” constraints for intensities above a threshold, $\alpha_{i,j}$
 - Cost function $g(I)$, cost per unit distance in type j regions of intensity I .
 - Total exposure parameter: Total travel (throughout R) cannot exceed $D_{i,j}^{max}$
 - Alternation parameters for exposure bursts:
 - Can travel $\leq d_{i,j}$ in region of type j if followed by travel of $\geq D_{i,j}$ outside regions of type j

Flows and Air Lanes:

RNP, Separation Parameters

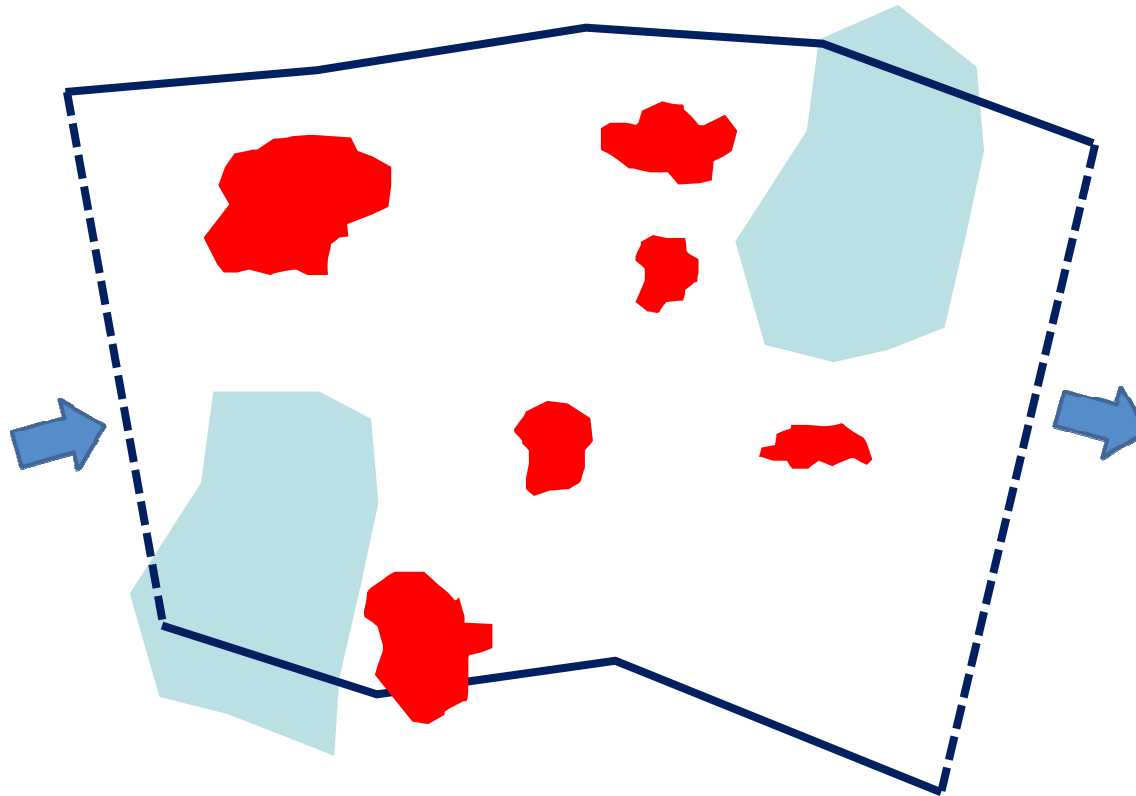


Model of Hard/Soft Constraints

- Hard, soft, and everything in between:
 - Each class i of aircraft (equipage, preferences, etc) has an *interaction profile* with each type j of weather event
- *Weather Impact Interaction Grid*
- Multiclass capacity

Model of Hard/Soft Constraints

- Simple, 2-class, 2-type example:
 - Class 1: Avoid type-1 (red) constraints (“Hard”), but can ignore type-2 (blue) constraints (“Soft”)
 - Class 2: Must avoid both type-1 and type-2 constraints (Hard and Soft)



Weather Impact Interaction Grid

Weather event type j

		<i>Weather event type j</i>			
		Icing	Turbulence	Fog	Visibility
<i>Aircraft class i</i>	1	Light OK Moderate: limit total exposure Extreme: no-go			
	2	Light: alternation parameters Moderate: No-go			
	3				

Stochastic Model of Weather

- The intensity, $W_j(x,y,z,t)$, of weather of type j is not known with certainty, but is given by a probabilistic forecast
- How to model the random function $W_j(x,y,z,t)$?

Probability of What?

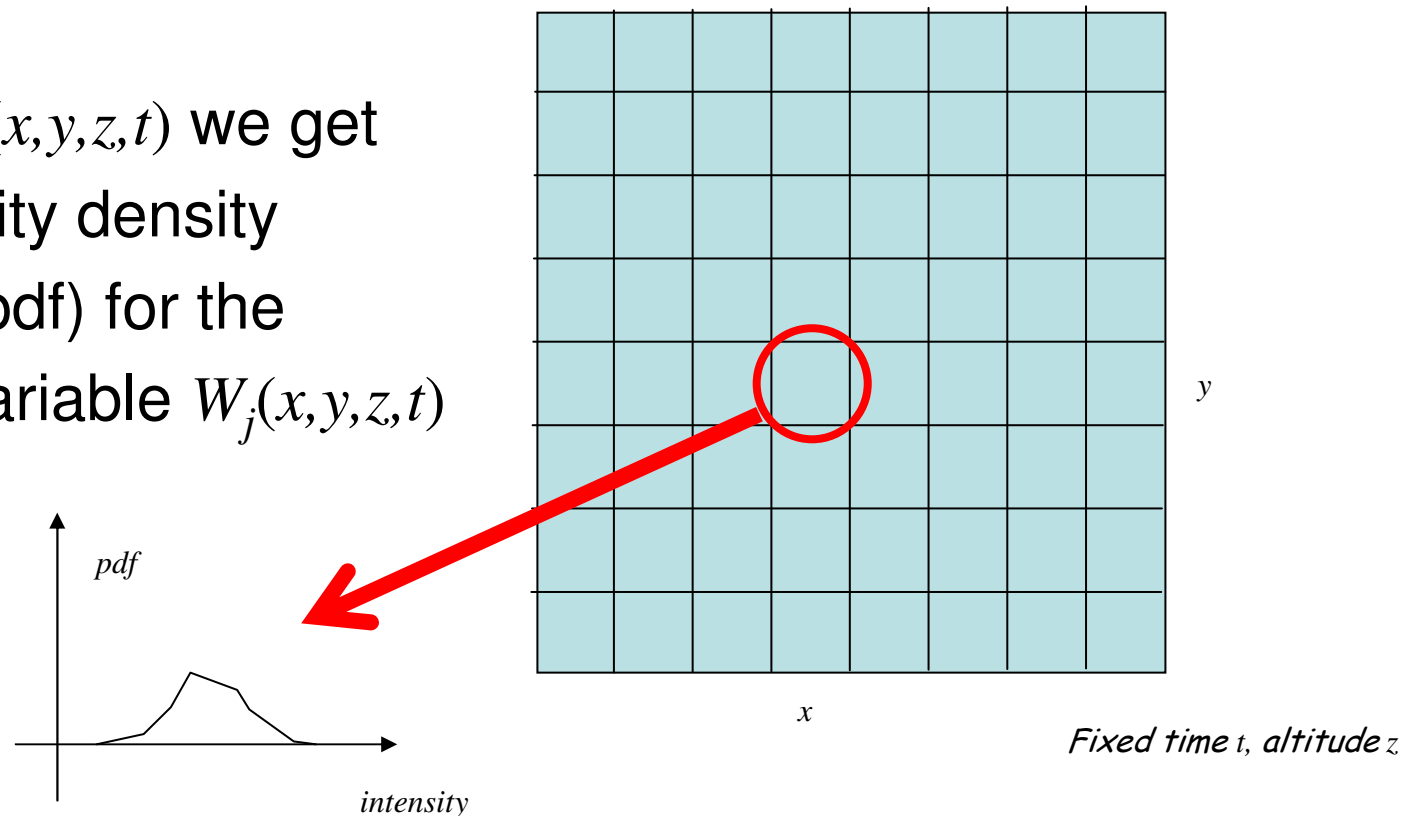
- Ambiguity in
 - timing & location
 - definition of “event”
 - communication
- Probability of
 - presence of weather hazard in space & time
 - hazard exceeding critical threshold intensity
 - structure & organization of weather hazard
- What do aviation users want?



Stochastic Model of Weather

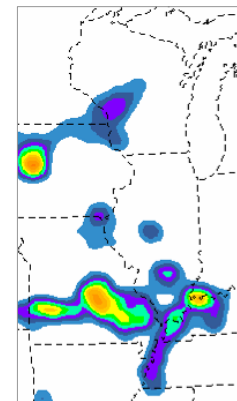
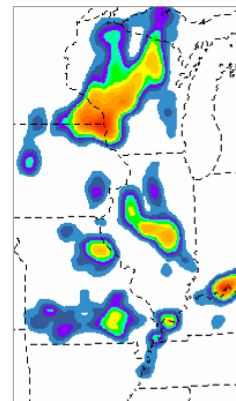
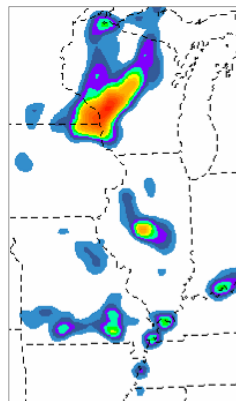
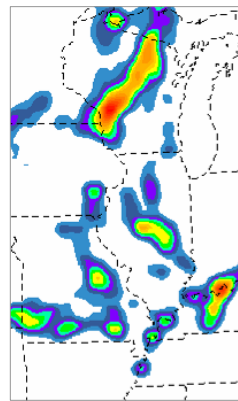
- One method: probabilistic pixel grid (or forecast of gridded pdf's):

- For each (x, y, z, t) we get a probability density function (pdf) for the random variable $W_j(x, y, z, t)$



Stochastic Model of Weather

- Another method: Ensemble of forecasts



...

Forecast:

F_1

F_2

F_3

F_4

...

Probability:

p_1

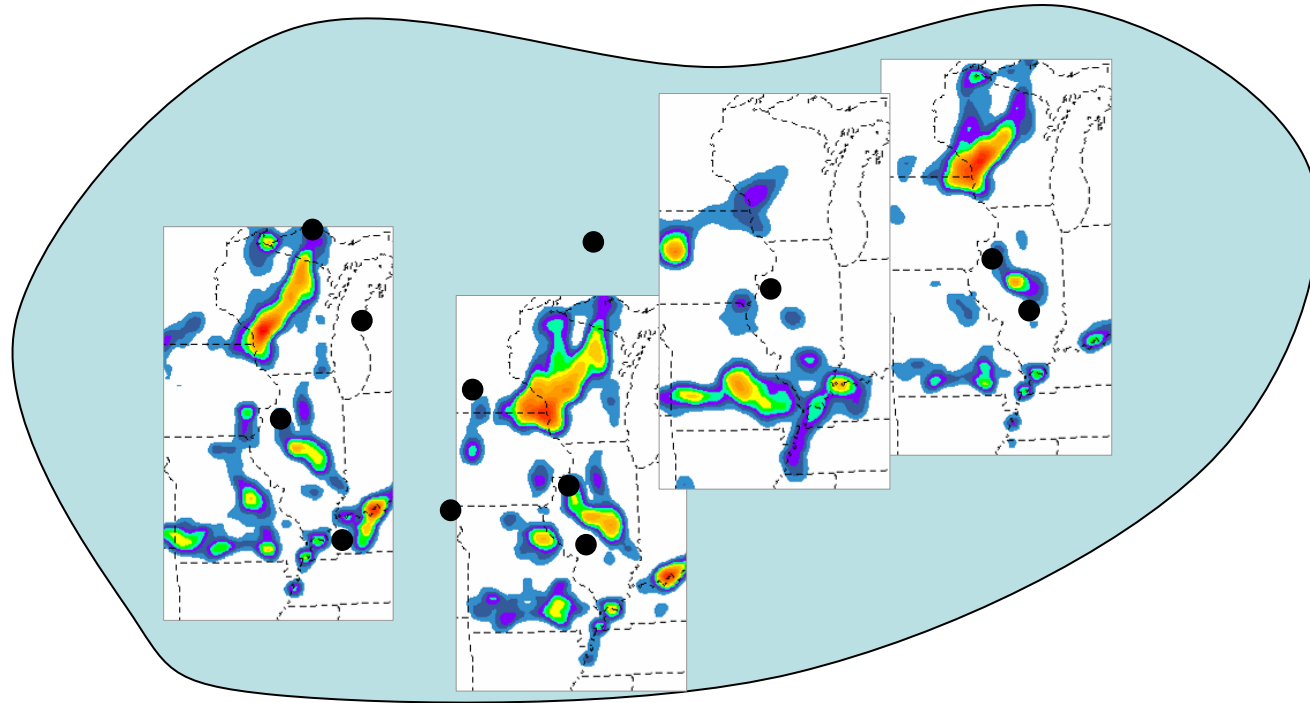
p_2

p_3

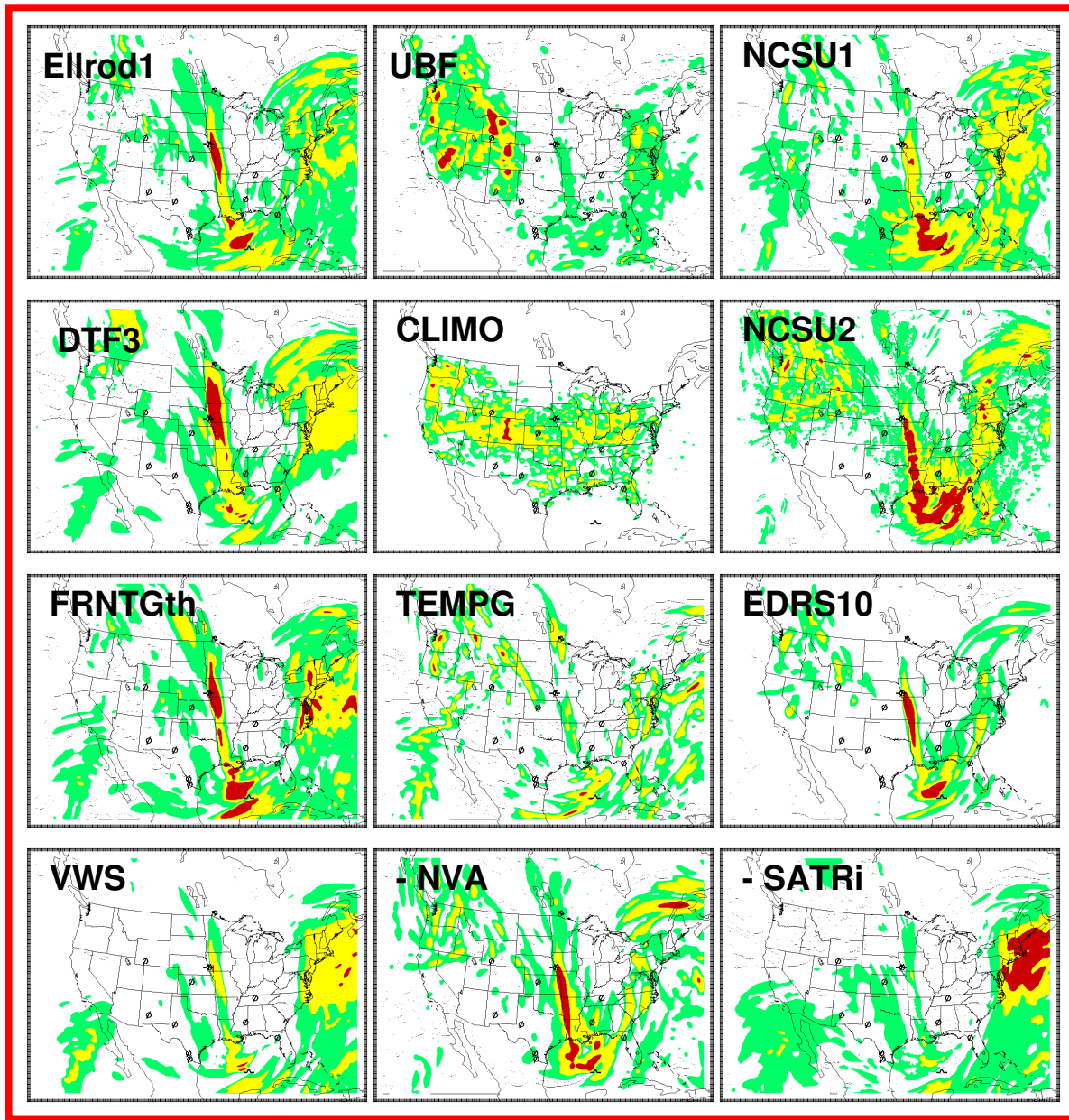
p_4

Discussion: How many? How to assess prior probabilities?

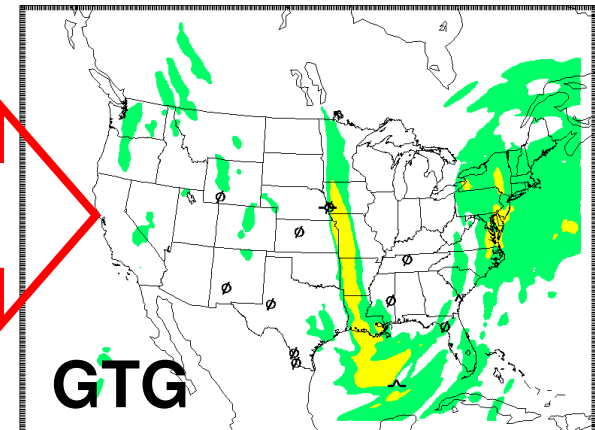
Stochastic Models: Ensembles



Space of all possible forecasts F : probabilities $p(F)$



Merging a variety
of **turbulence
diagnostics**
into GTG

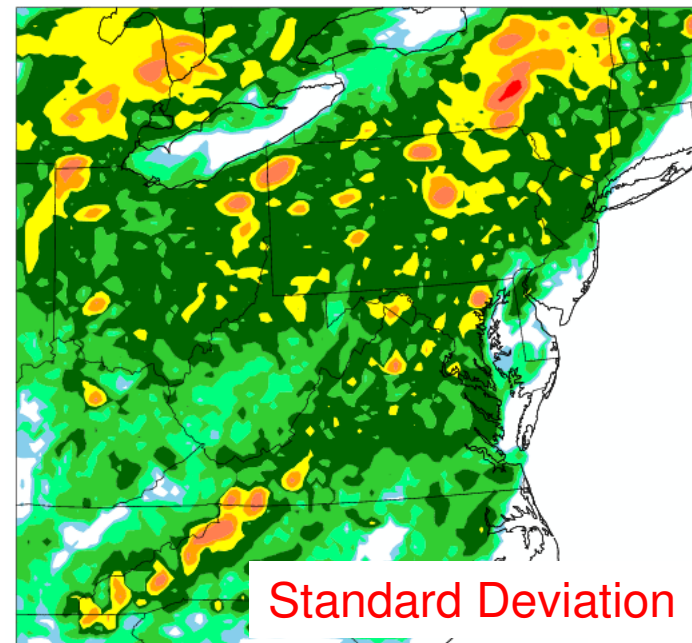
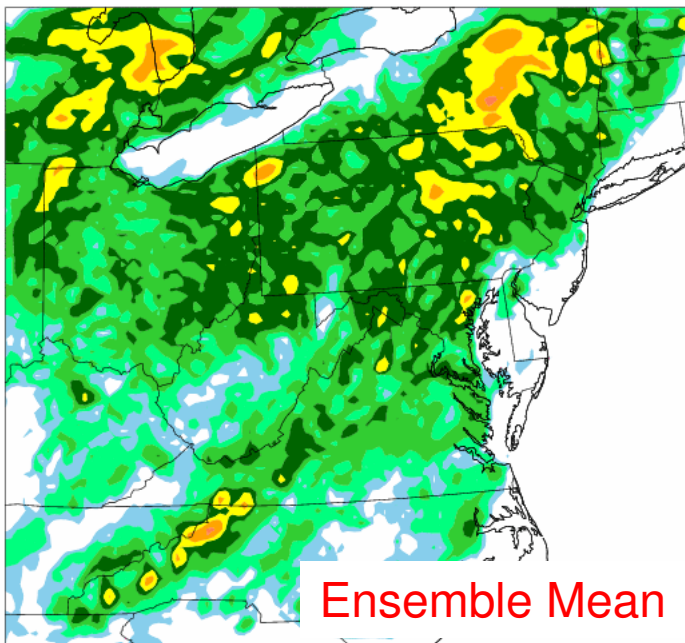
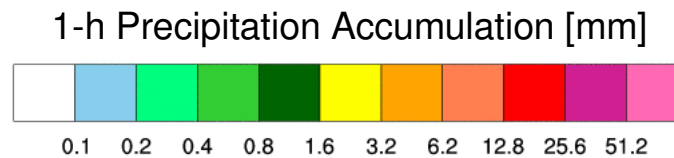
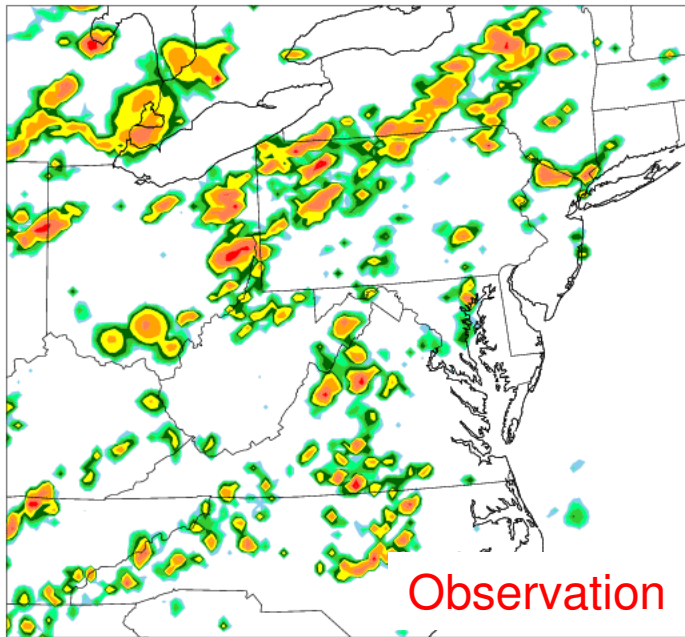


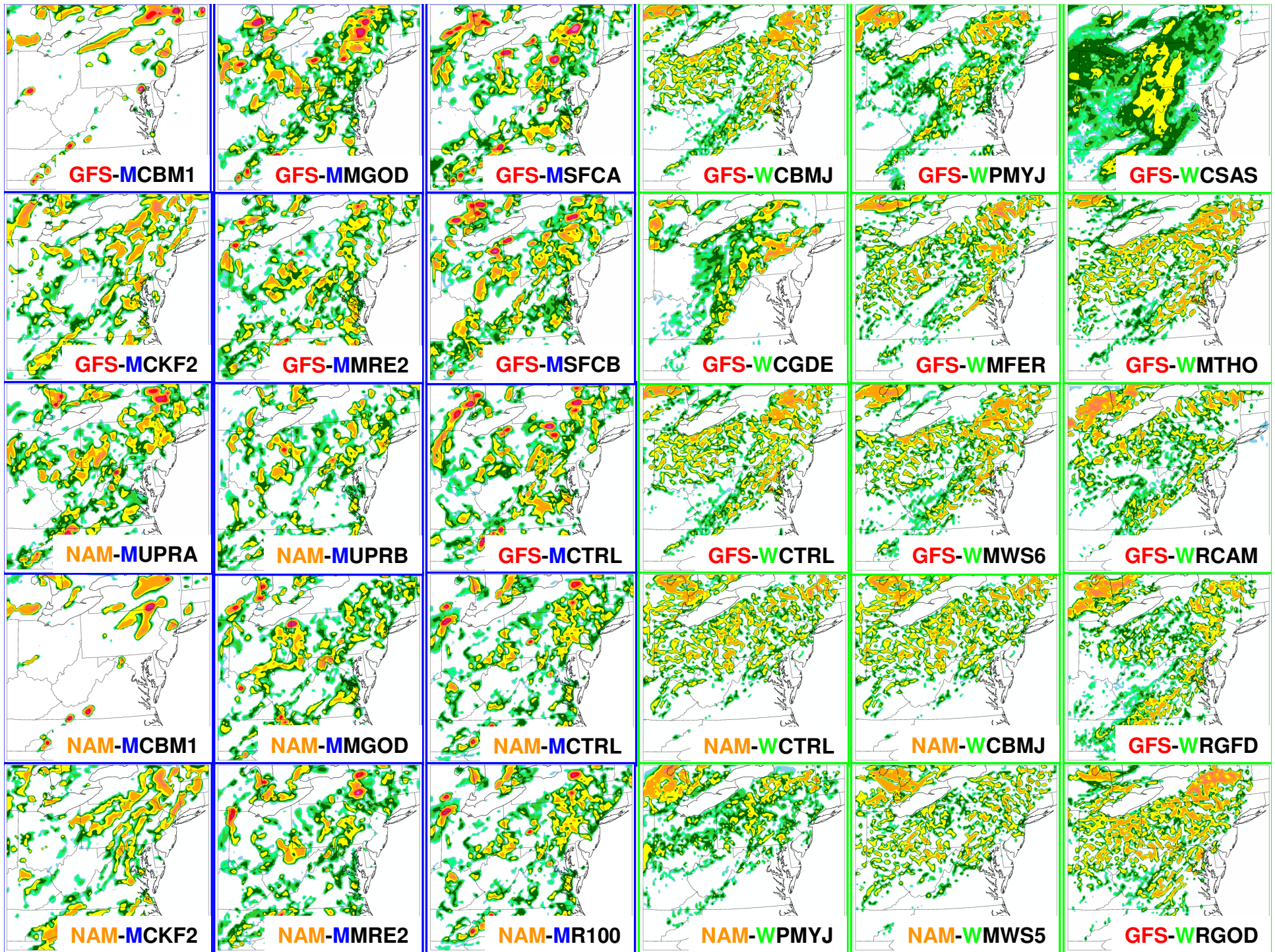
6 h forecast valid at 5 Feb 2006 00Z

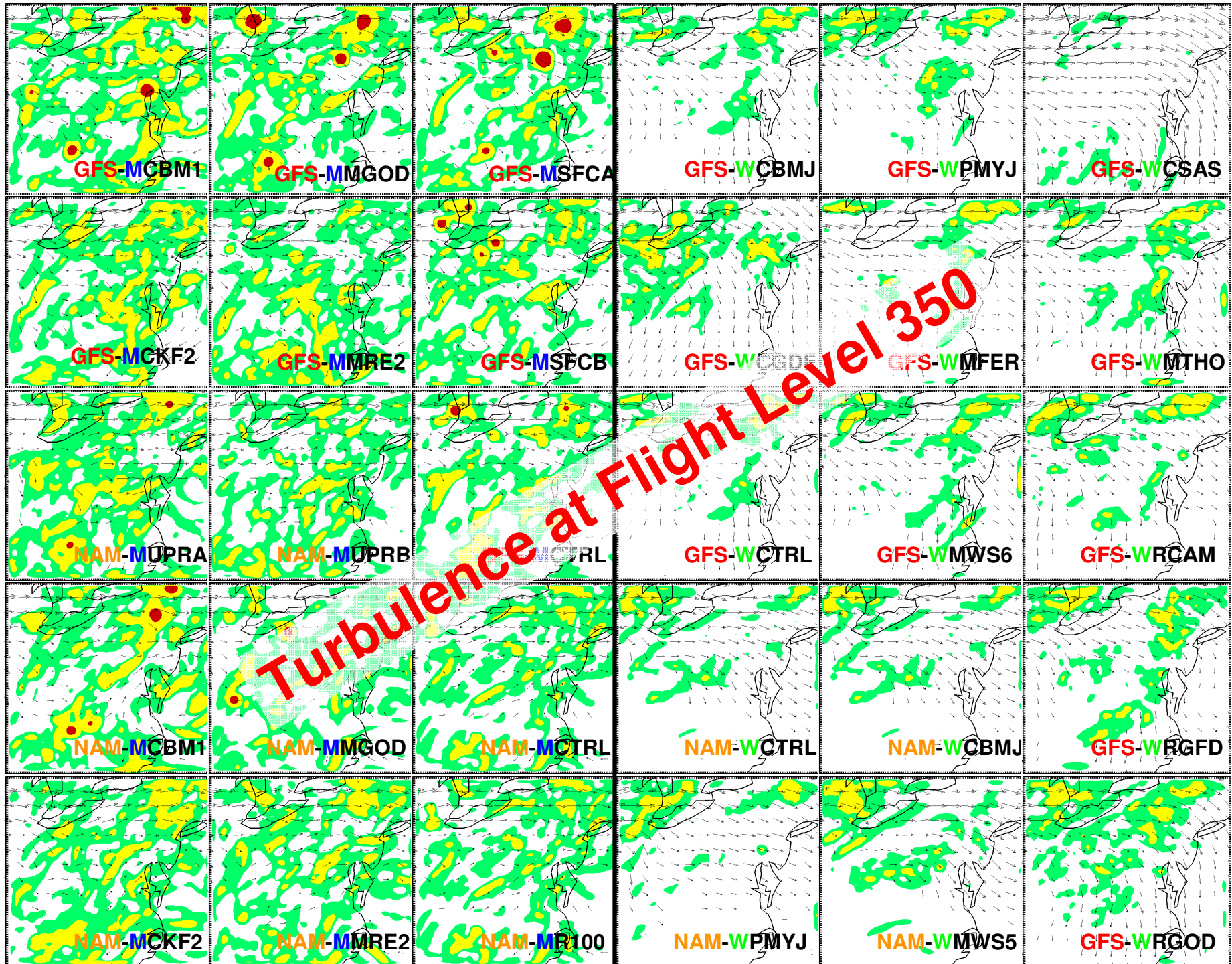
Flight level: 350

provide a measure of
“forecast confidence”

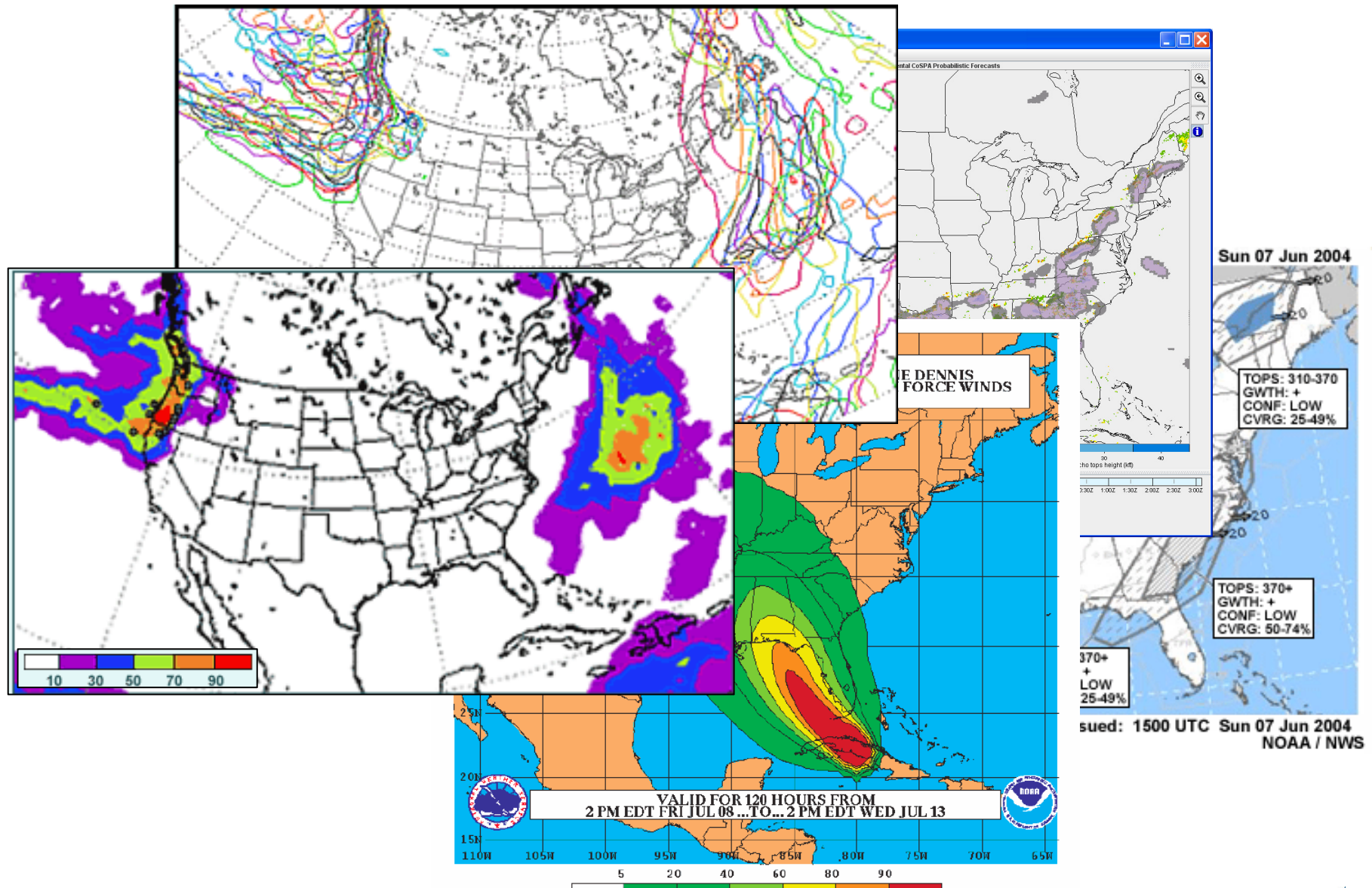
9 h Ensemble Forecast valid for 27 June 2007 at 21 UTC







Visualization of Ensemble Forecasts



Stochastic Model of Weather

- Issue: Grid does not explicitly model spatial and temporal dependencies/correlations

Forecast F_1 , prob = 0.5

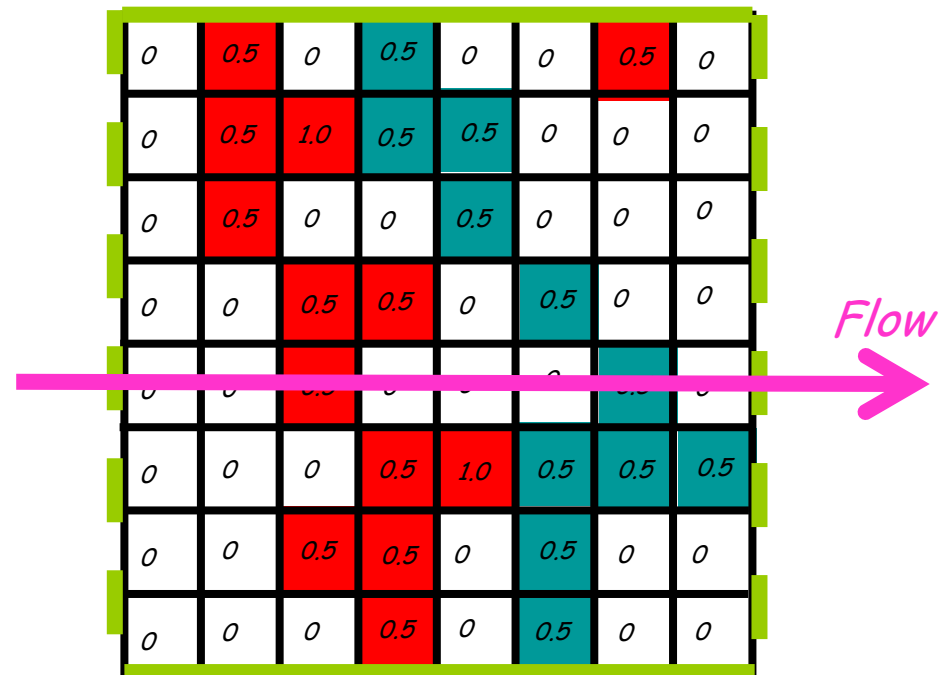
Forecast F_2 , prob = 0.5

Each pixel has a simple Bernoulli distribution, with $P(\text{blocked})$ given by the values (0, 0.5, 1.0) shown

$P(\text{flow is feasible}) = ?$

$0.5 ? (0.5)^2 ?$

Ensemble model: Prob = 0



Variations on a Forecast

- Uncertainty on when exact a weather event impacts and moves through a region:

Probabilities 0.25 each

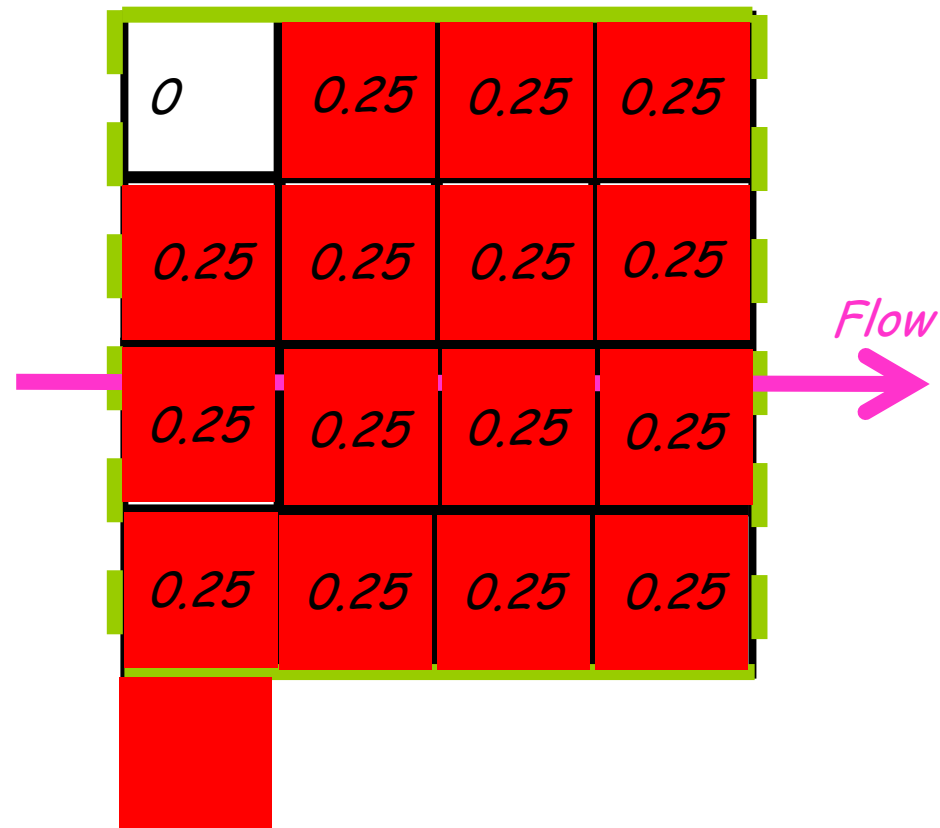
$P(\text{flow is feasible}) = ?$

$(0.75)^4 ?$ (indep)

0.25 ?

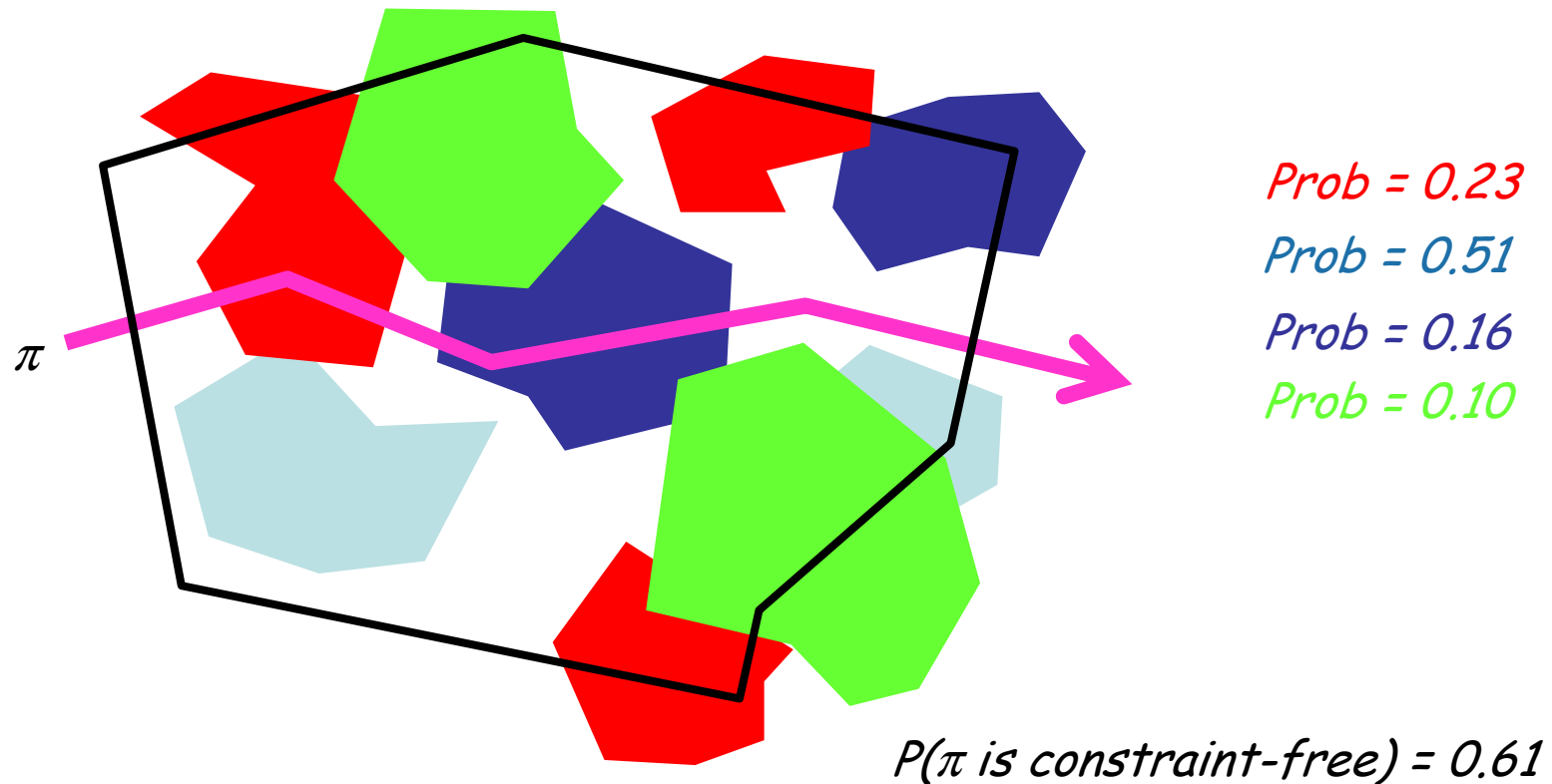
BUT, $P(\text{there is east-west capacity of at least 2 lanes}) = 1$

NOTE: $P(\text{north-south lane}) = 0 !$



Interactions with Probabilistic Weather

- What is the probability a route π is feasible with respect to constraints?

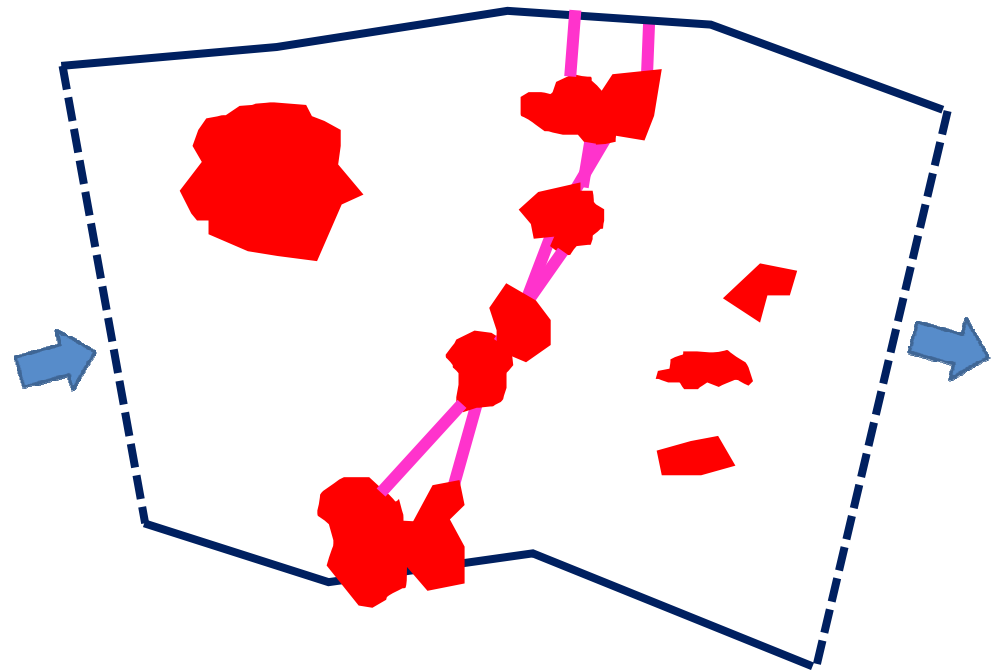


Variations on Forecast



Capacity Estimation: Probabilistic Weather

- For capacity estimation, exact shape of weather impact region is not as significant as its “porosity”



Clustered Ensemble Models

- Use variations on seed forecasts
- Much fewer seeds
- Each cluster of forecasts is based on a variation model centered on a seed:
 - Vary time (errors in time)
 - Vary intensity map (shift up/down), thereby impacting coverage
 - Vary translation (x, y)
 - Vary echo tops

•What distributions to use for variations on seed forecasts? ΔT , $\Delta \text{Coverage}$, $\Delta \text{Translation}$, ΔTops , etc.